The Topology of Politics

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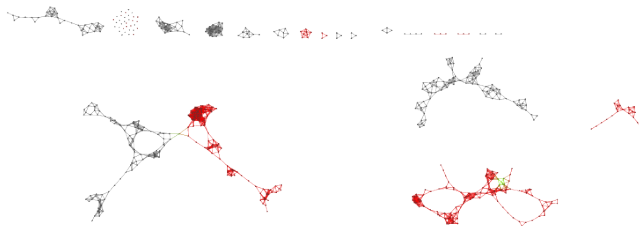
Royal Institute of Technology
Stockholm, Sweden
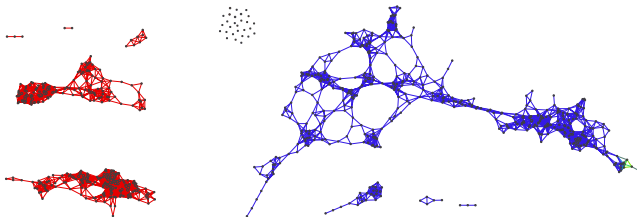

KTH Computer Science
and Communication

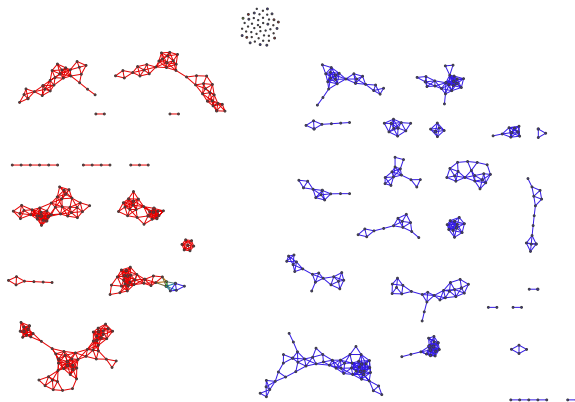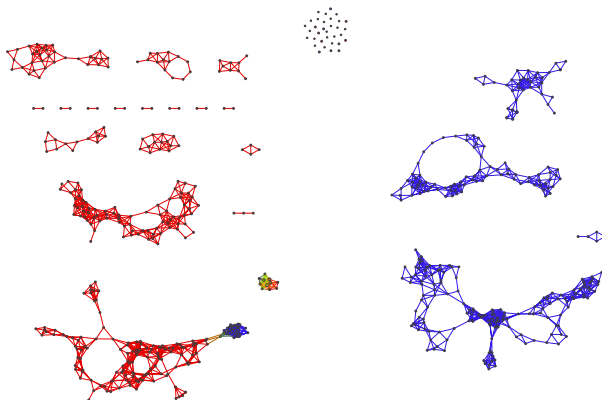15 October 2012

Southern Democrats

Obama wins

Health care reform
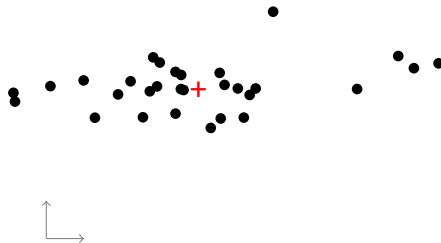
Consolidation

Outline

1. Data analysis

2. Data analysis in politics

3. Wherefore topology?

Shape of data

Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

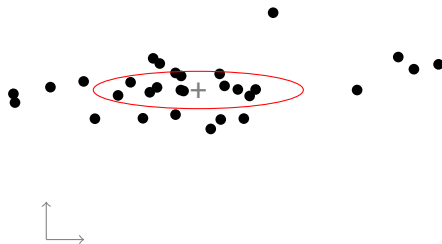Mean (centroid) tells us *where* the data is located.

Shape of data

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Fundamental data analysis techniques

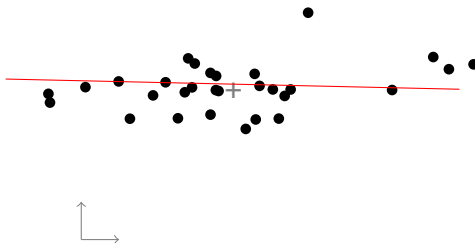Standard deviation tells us how spread out the data is.

Shape of data

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Fundamental data analysis techniques

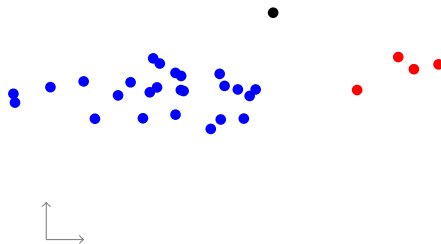Regression analyses fit the data to an easy to analyze model.

Shape of data

Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Cluster analysis divides the data into its connected components.
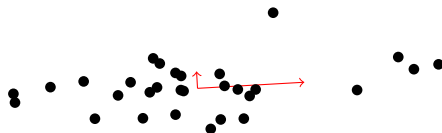
Shape of data

Fundamentally, data analysis is the task of describing the shape of data:

Fundamental data analysis techniques

Principal Component Analysis (and other dimension reduction techniques) give new coordinates that more faithfully represent the data.

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The shape of politics

Data analysis has long pedigree in political science.

- Tufte discusses improvements to techniques in a 1969 paper
- Gallups, polling, and voter prediction leverages more and stronger analysis techniques every year.

Entered into politics in the 90's. Example of the type of analyses done: PCA of votes in House of Congress.
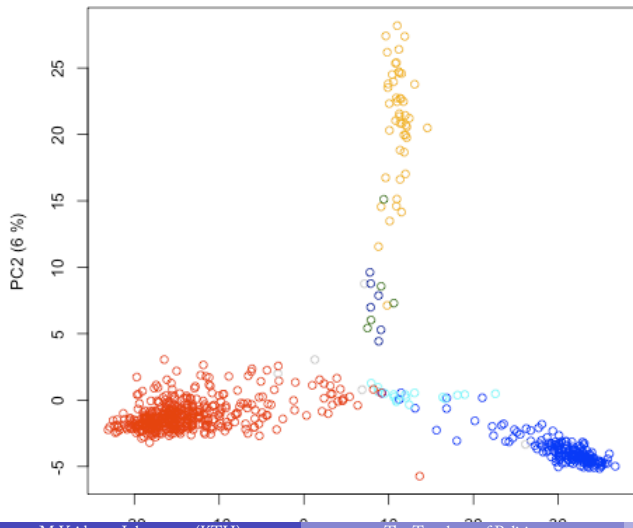
The shape of politics

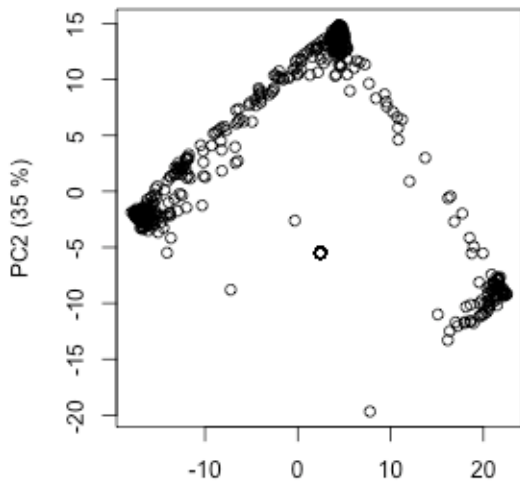We shall focus on one area of use: the analysis of parliamentary bodies.

Dataset

For a parliamentary session, N members of parliament vote on M issues.
Votes form an $N \times M$-matrix V of votes cast. Encoded $+1$ for Yea, -1 for Nay
and 0 for all other results.

c.f. Dan Rockmore's work using similarly constructed datasets.

The shape of politics

The shape of politics

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Wherefore topology?

Topology gives qualitative information

Topology is about geometric properties not dependent on a metric:
How many pieces? Are there holes? Bubbles? Can you get turned around
while moving?

Topology captures continuity, connectedness, nearness

In particular, the non-dependence on a metric helps if metrics are
ill-motivated, eg phylo-genetics.

A topological analysis method

In a recent PhD thesis at Stanford [Singh, '08], a topological method for data analysis was introduced.

Fundamental topological result: Nerve lemma

Suppose a space X is subdivided $X = \bigcup_i X_i$ into *contractible* (read simple) components.
Then X is equivalent to the *nerve* of the covering.

The nerve of a covering
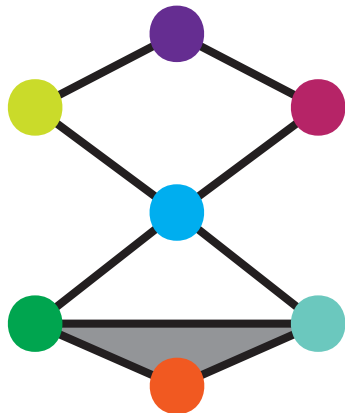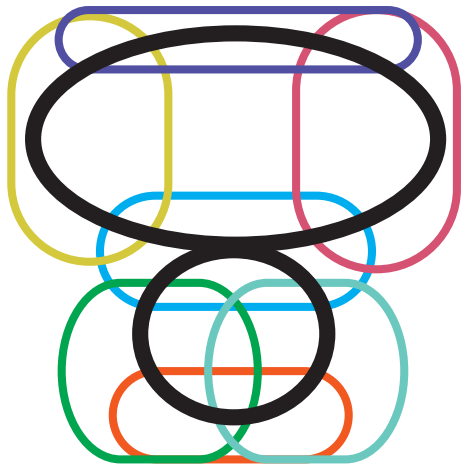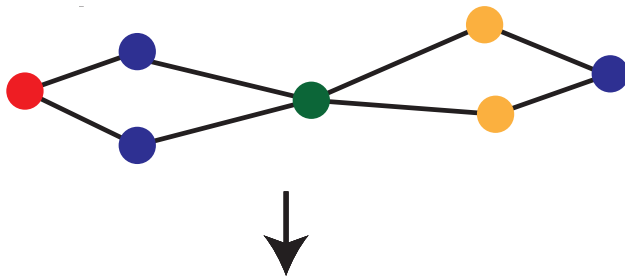
Topological application
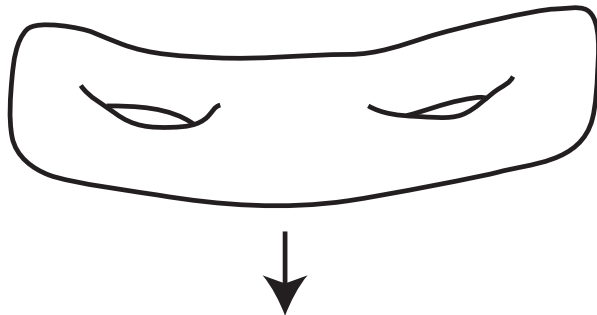
Topological application
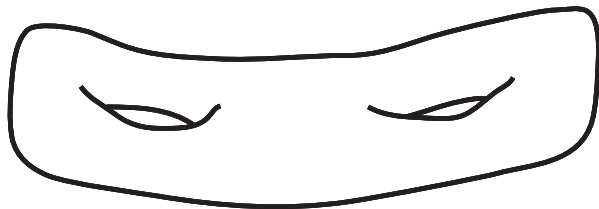
Topological application
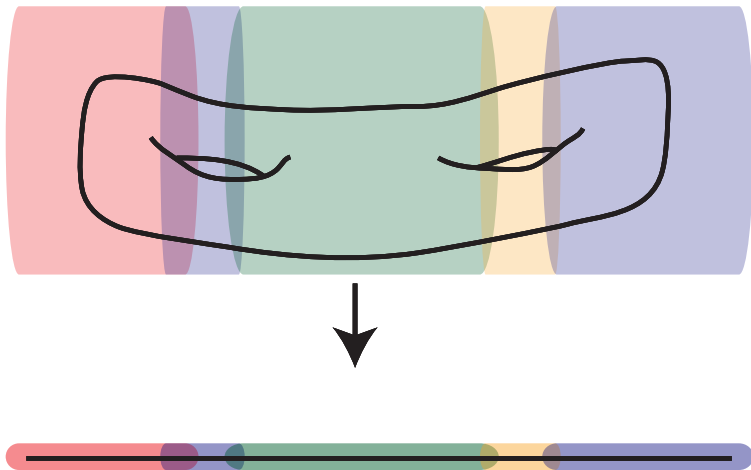
Topological application
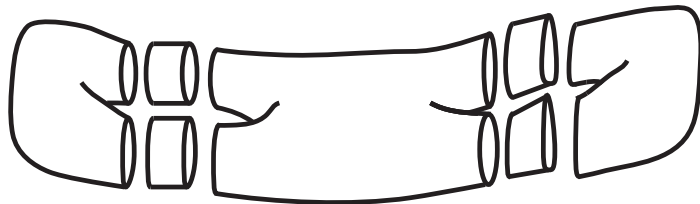
Topological application

Translate topology to statistics

Continuous function	Measurement function on datapoints
Covering of target space	Covering of datapoints
Preimages	Preimages
Connected components	Clusters
Nerve complex	Mapper diagram

Mapper algorithm
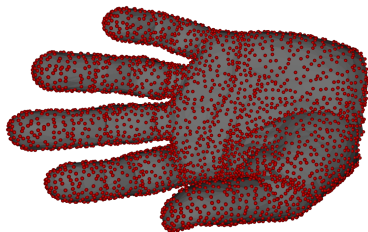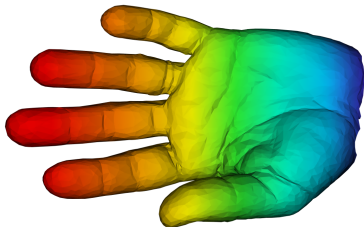
Mapper algorithm
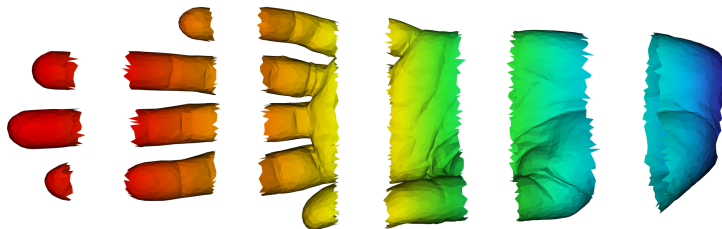
Mapper algorithm
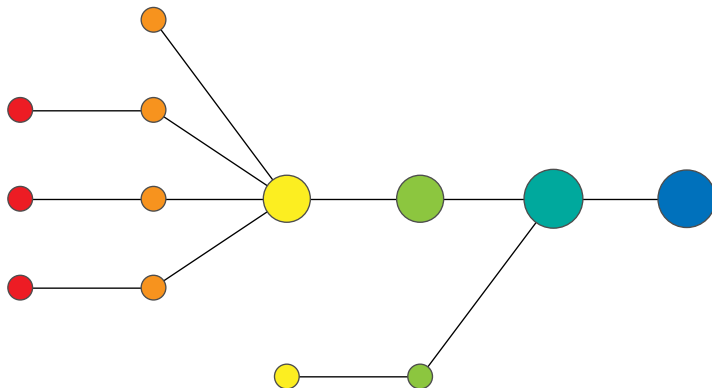
Mapper algorithm

Mapper algorithm

Implementation

This method is provided in a software package currently marketed by Ayasdi.
Startup company founded by Gurjeet Singh (original thesis on Mapper) and Gunnar Carlsson (thesis advisor).

UK Parliament

Parliamentary period 2001–2005. Conservative
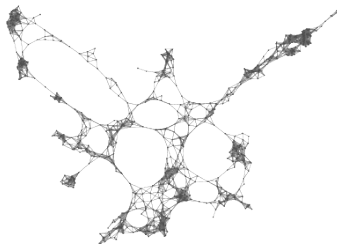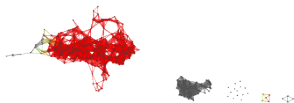
UK Parliament

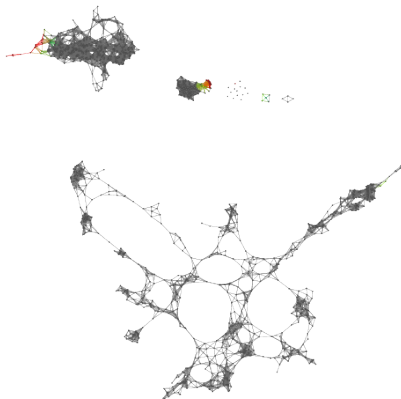Parliamentary period 2001–2005. Labour
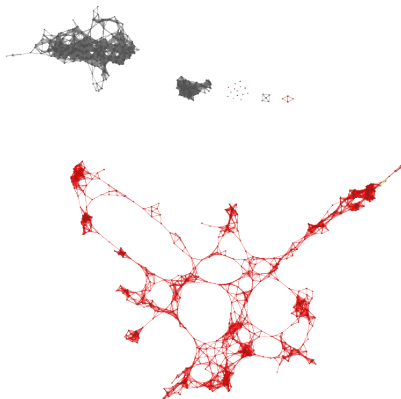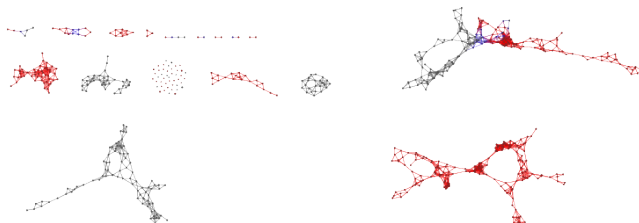
UK Parliament

Parliamentary period 2001–2005.   Liberal Democrats
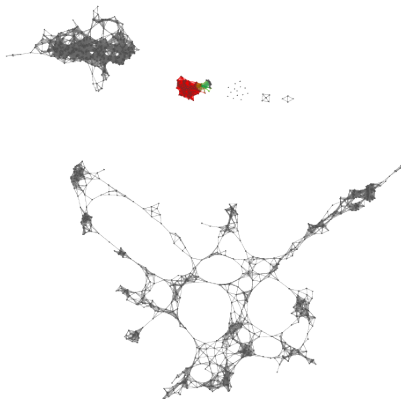
UK Parliament

Parliamentary period 2001–2005.   Regional parties

House of Representative.

1991

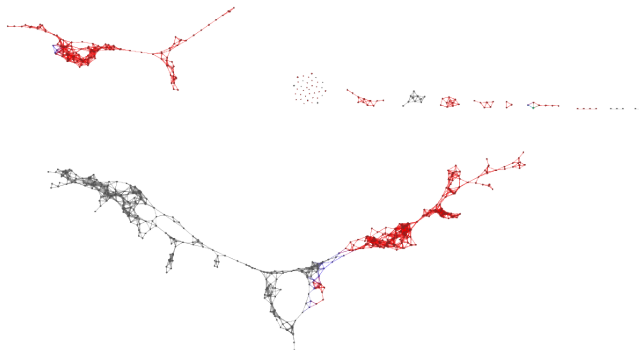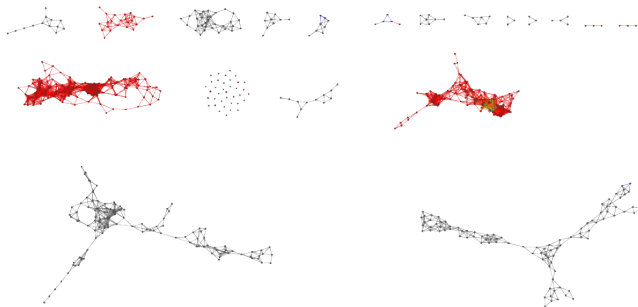# House of Representative.

1992
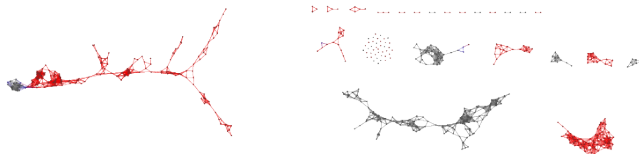
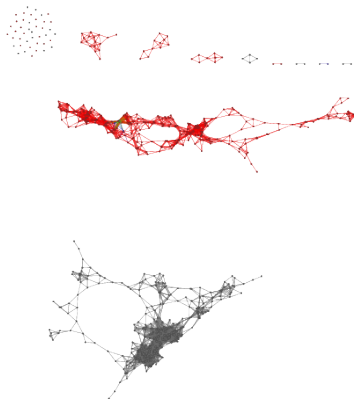# House of Representative.

1993
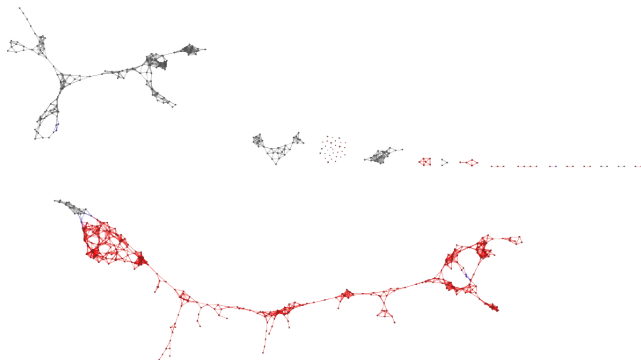
House of Representative.
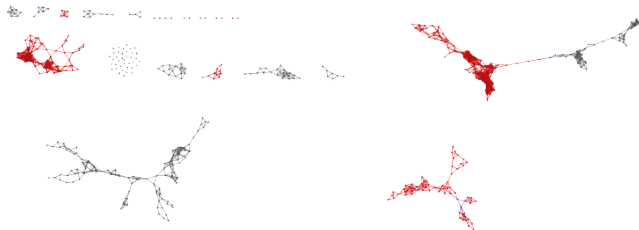
1994

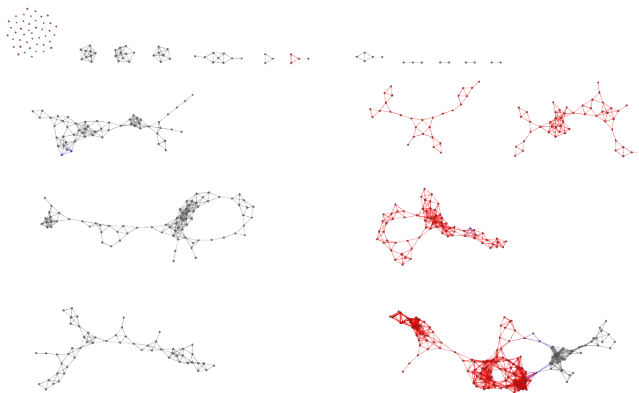# House of Representative.

1995

House of Representative.
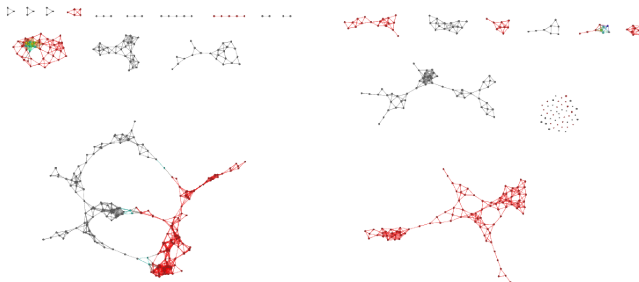
1996

House of Representative.

1997
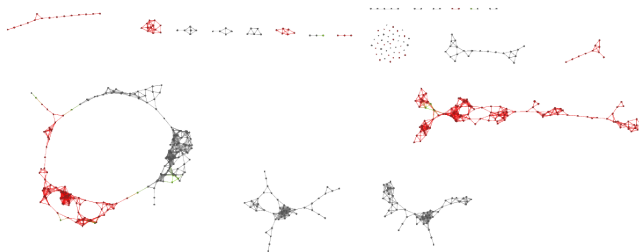
House of Representative.

1998

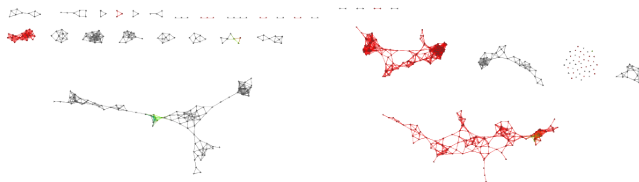# House of Representative.

1999

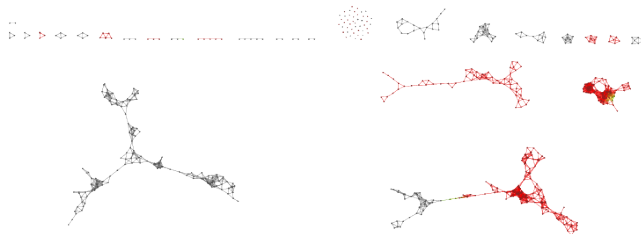# House of Representative.
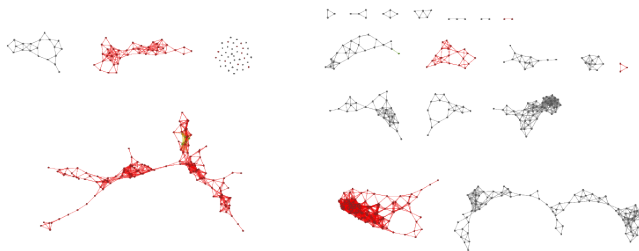
2000

House of Representative.
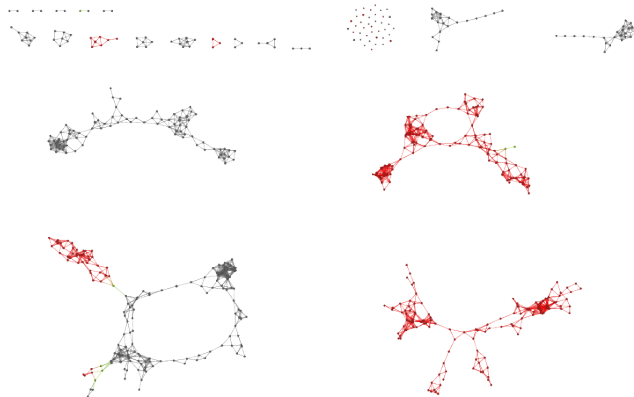
2001

House of Representative.
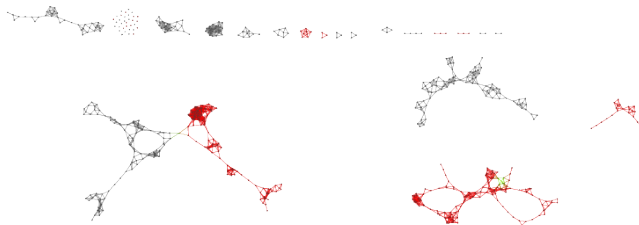
2002

House of Representative.

2003
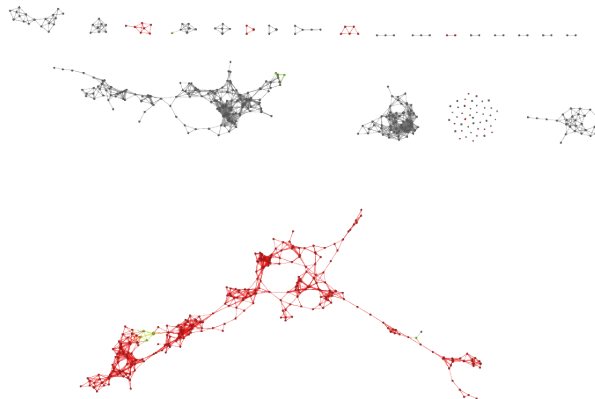
House of Representative.

2004

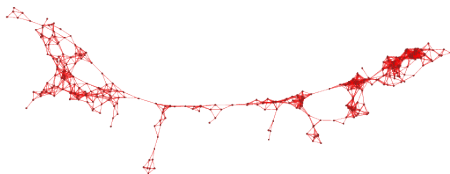# House of Representative.
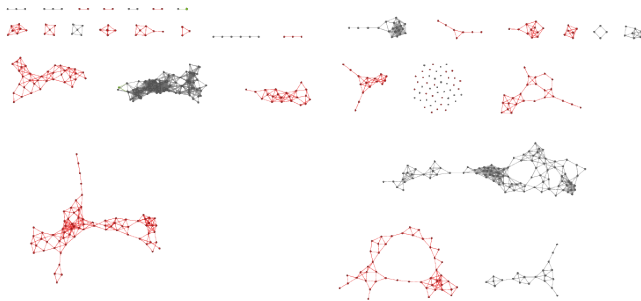
2005

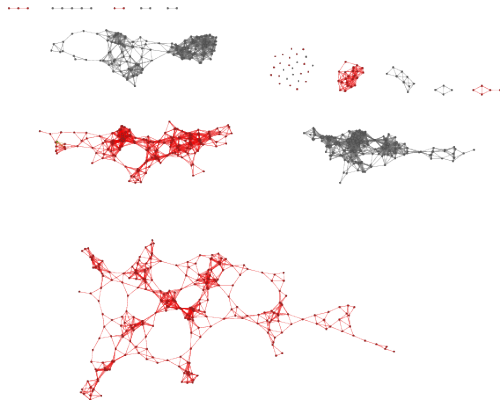# House of Representative.

2006

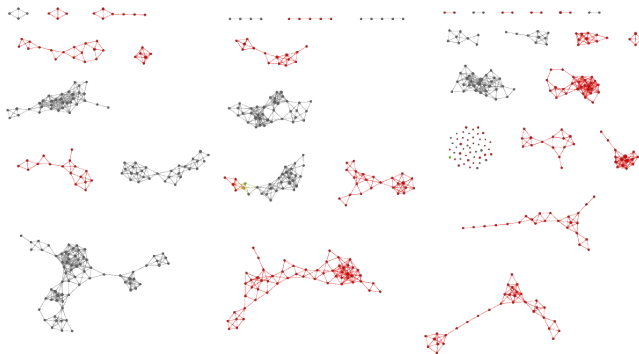# House of Representative.

2007

House of Representative.

2008

House of Representative.

2009

House of Representative.

2010

Questions?

Future directions

- More parliaments. We have (mostly un-analyzed) data for:
    - Sweden
    - European Union
    - Canada
    - US Senate

- Network analysis: who co-sponsors with whom, what are the parliamentary cliques?

- Flow analysis: FEC has a database over campaign donations; what can we tell about the flow of contributions?

- Meme spread: who takes over turns of phrase from whom?